

Supporting Information

## **Efficiency Analysis of the Discrete Element Method Model in Gas-Fluidized Beds**

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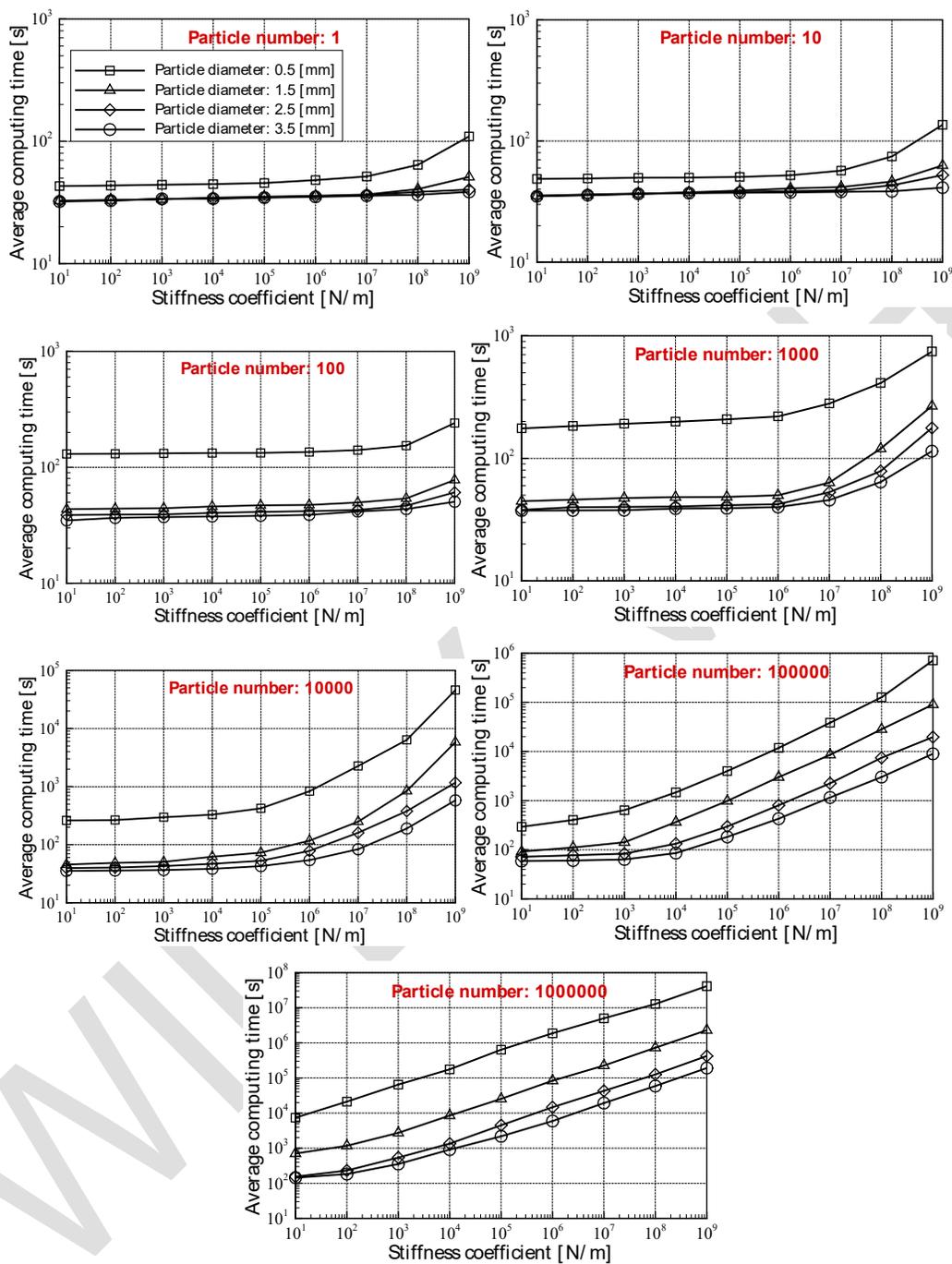
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**Table S1.** Calculation of penetration depths for glass collision partners with different particle diameters and relative velocity of 10 m/s

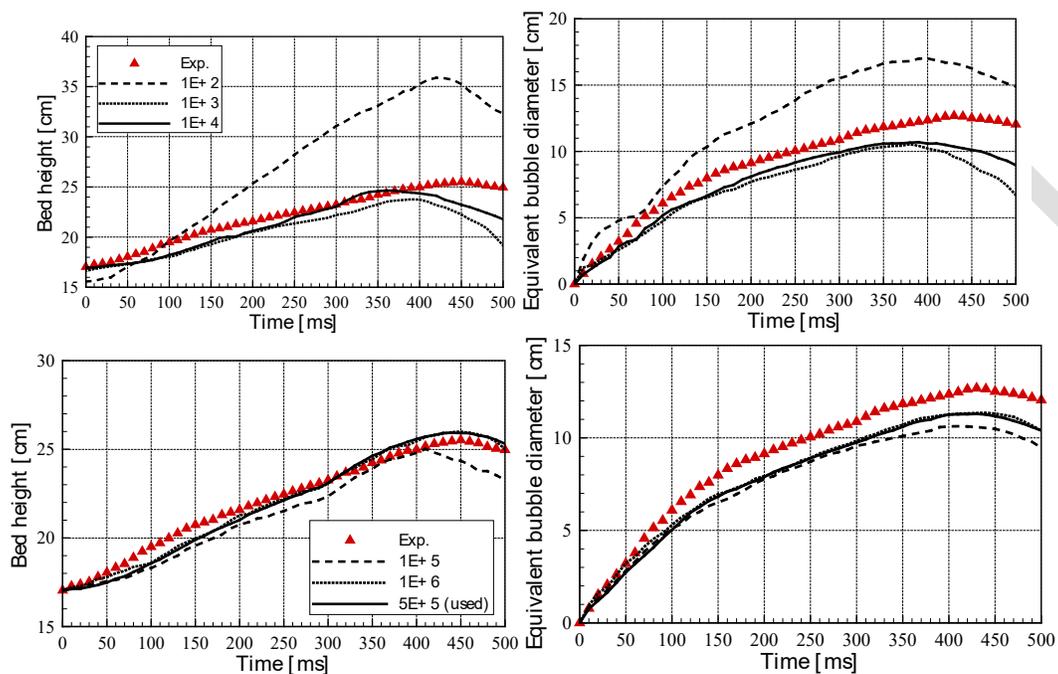
Stiffness coefficients	Penetration depths			
	$d_p = 0.5$	$d_p = 1.5$	$d_p = 2.5$	$d_p = 3.5$
$k^n = 10^2$	14	73	160	260
$k^n = 10^4$	1.4	7.3	16	26
$k^n = 10^6$	0.14	0.73	1.6	2.6
$k^n = 10^8$	0.014	0.07	0.16	0.26

**Table S2.** Calculation of minimum normal stiffness coefficients at different particle diameters, relative velocities, and maximum penetration

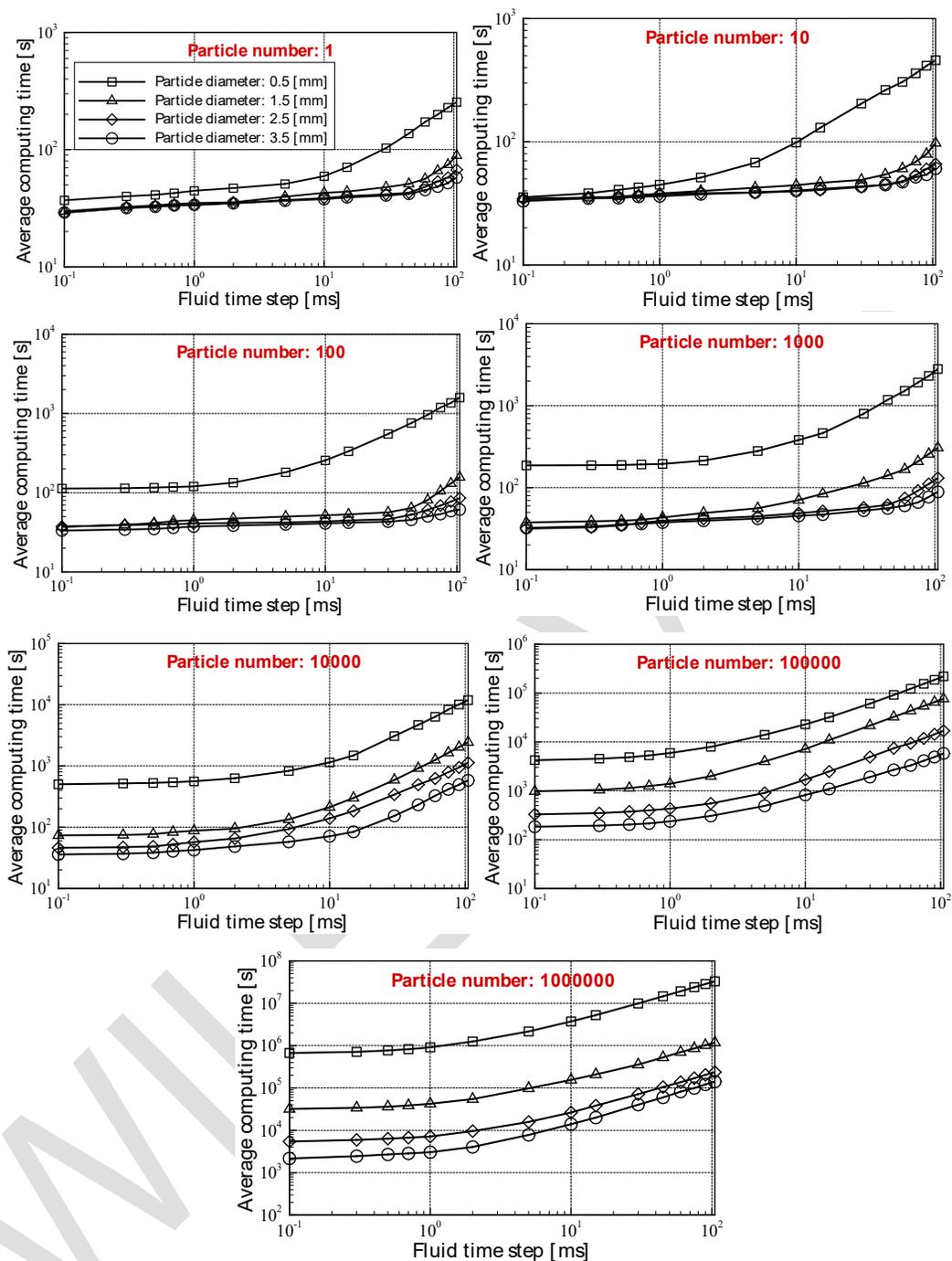
Stiffness coefficients	Particle diameters			
	0.5	1.5	2.5	3.5
$k^n (u_{\max}^n = 10 \text{ [m/s]})$	$5.1 \times 10^6$	$5.1 \times 10^6$	$5.1 \times 10^6$	$5.1 \times 10^6$
$k^n (u_{\max}^n = 5 \text{ [m/s]})$	$6.3 \times 10^5$	$6.3 \times 10^5$	$6.3 \times 10^5$	$6.3 \times 10^5$
$k^n (u_{\max}^n = 2 \text{ [m/s]})$	$4.1 \times 10^4$	$4.1 \times 10^4$	$4.1 \times 10^4$	$4.1 \times 10^4$



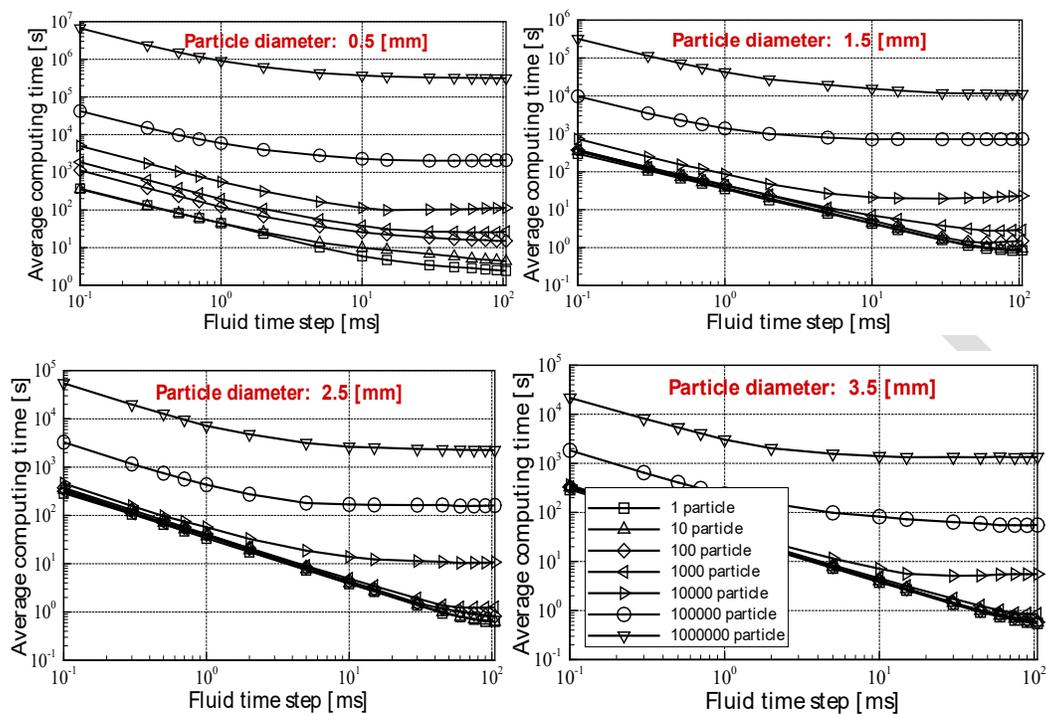
**Figure S1.** Influence of stiffness coefficient variation on the average computing time per time step at different particle diameters and various particle numbers



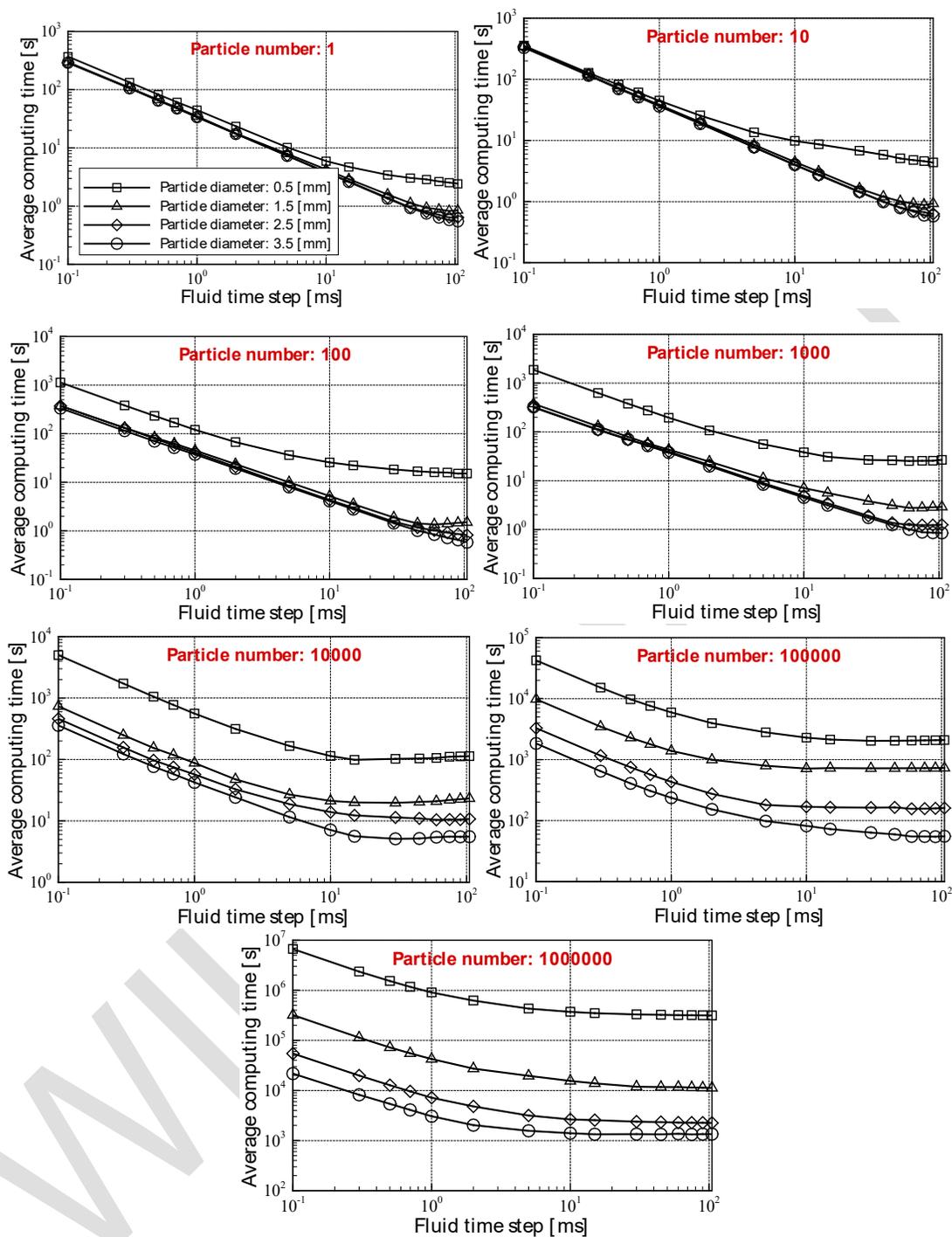
**Figure S2.** Influence of the stiffness coefficient variation on the simulation accuracy of the Euler-Lagrange/DEM model (number of particles is 36500 and the particle diameter is 2.5 mm for a mass flow rate of 0.006 kg/s)



**Figure S3.** Influence of fluid time step variation on the average computing time per time step at different particle diameters and various particle numbers



**Figure S4.** Influence of fluid time step variation on the average computing time per one millisecond at different solid loadings and various particle diameters



**Figure S5.** Influence of fluid time step variation on the average computing time per one millisecond at different solid loadings and various particle diameters